

Year 8 Maths – Homework Booklet

Autumn 1 Booklet 3

Algebra – Algebraic manipulation



Name: _____

Class: _____

Due Date: _____



1) $9 \times 6 =$

13) $3 \times 9 =$

2) $10 \times 10 =$

14) $32 \div 8 =$

3) $5 \times 7 =$

15) $20 \div 4 =$

4) $1 \times 7 =$

16) $9 \times 3 =$

5) $5 \times 9 =$

17) $4 \times 12 =$

6) $5 \times 4 =$

18) $8 \times 7 =$

7) $11 \times 3 =$

19) $8 \times 9 =$

8) $10 \times 11 =$

20) $99 \div 11 =$

9) $12 \times 12 =$

21) $50 \div 5 =$

10) $9 \div 3 =$

22) $11 \times 10 =$

11) $7 \times 6 =$

23) $1 \times 4 =$

12) $36 \div 3 =$

24) $5 \times 10 =$

Algebraic manipulation

Name: _____

1 Simplify the expressions.

a) $11a - 6a$

☐

1 mark

b) $7b - 2c + 3c + b$

☐

1 mark

c) $4d \times 5d$

☐

1 mark

d) $\frac{18f}{9}$

☐

1 mark

2 Match the statements to the expressions. z divided by 8

$8 - z$

8 divided by z

$z - 8$

8 less than z

$\frac{8}{z}$

 z less than 8

$\frac{z}{8}$

☐

2 marks

3**a)** Expand $2(w + 12)$.

1 mark

b) Expand $5t(t - 1)$.

1 mark

c) Factorise fully $30y - 24$

1 mark

4Work out the values of the expressions when $p = -4$ and $q = 5$ **a)** $6p + q$

1 mark

b) pq

1 mark

c) $3p^2$

1 mark



1) $108 \div 9 =$

13) $24 \div 3 =$

2) $12 \div 4 =$

14) $12 \times 7 =$

3) $56 \div 7 =$

15) $80 \div 10 =$

4) $14 \div 2 =$

16) $12 \times 10 =$

5) $3 \times 2 =$

17) $10 \times 5 =$

6) $4 \times 7 =$

18) $60 \div 12 =$

7) $9 \times 11 =$

19) $7 \times 4 =$

8) $2 \times 12 =$

20) $2 \times 4 =$

9) $21 \div 7 =$

21) $14 \div 7 =$

10) $11 \times 7 =$

22) $11 \times 4 =$

11) $11 \times 12 =$

23) $5 \times 5 =$

12) $3 \times 6 =$

24) $45 \div 5 =$

5

Expand and simplify the expression.

$$8(5r - 2) - 3(2 + 5r)$$



2 marks

6

Tick the expressions.

$$A = \pi r^2$$

$$5(a + b) \equiv 5a + b$$

$$P = 5(a + b)$$

$$\pi r^2$$

$$5(a + b)$$

$$5a + b$$



2 marks

7

Factorise $x^2 + 3x - 40$

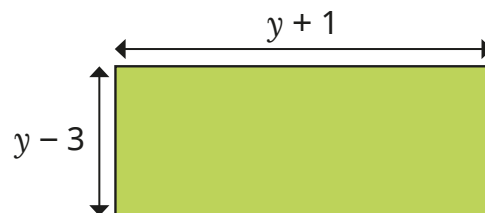
E



2 marks

8

Write an expression for the area of the rectangle, giving your answer in the form $x^2 + bx + c$.



2 marks

NUMBER...

Algebraic manipulation

What do I need to be able to do?

- Form algebraic expressions
- Identify and use formulae, expressions, identities and equations
- Simplify expressions
- Use directed number with algebra
- Substitution with directed number
- Expand a single bracket
- Factorise into a single bracket
- Expand single brackets and simplify
- Expand double brackets (E)
- Factorise quadratic expressions (E)

Keywords

Tier 2:

Variable: a symbol for a number we don't know yet

Expression: numbers, symbols and operators grouped together to show the value of something

Identity: An equation where both sides have variables that cause the same answer includes $\equiv$

Substitute: replace one variable with a number or new variable

Equivalent: something of equal value

Coefficient: a number used to multiply a variable

Equation: a statement that the values of two mathematical expressions are equal (indicated by the sign =)

Formula: A mathematical relationship/ rule given in symbols

Tier 3:

Highest Common Factor (HCF): the biggest factor (or number that multiplies to give a term)

Using letters to represent numbers

$5 + 5 + 5$	$y + y + y + y$	$20 - h$
3×5	$y \times 4$	$\frac{20}{h}$
5×3	$4 \times y$	$\frac{20}{h}$
	$4y$	$\uparrow$
Addition and multiplication can be done in any order Commutative calculations	4 lots of 'y'	20 shared into 'h' number of groups

Substitution into expressions

$4y \longleftarrow 4 \text{ lots of 'y'}$

If $y = 7$ this means the expression is asking for 4 'lots of' 7

4×7 OR $7 + 7 + 7 + 7$ OR 7×4 = **-28**

eg: $y - 2$
 $= 7 - 2 = 5$

$2(x + 3)$ Put the expression into a function machine

INPUT $\rightarrow$ $+3$ $\rightarrow$ $\times 2$ $\rightarrow$ OUTPUT

If $x = 10$ $10 + 3 = 13 \dots 13 \times 2 = 26$

Expand double brackets

$2(x + 2) \equiv 2x + 4$

Algebra tiles can represent a binomial expansion
Has two terms

$(x + 3)(x + 3) \equiv x^2 + 6x + 9$

This is a quadratic. It has four terms which simplified to three terms

The order of the brackets has no impact on the outcome
eg $(x + 3)(3 + x)$

Collecting like terms $\equiv$ symbol

The $\equiv$ symbol means equivalent to
It is used to identify equivalent expressions

Collecting like terms

Only like terms can be combined

$4x + 5b - 2x + 10b$

$(4x) + (5b) - (2x) + (10b)$

$2x + 15b$

Common misconceptions

$$2x + 3x^2 + 4x \equiv 6x + 3x^2$$

Although they both have the x variable x^2 and x terms are un-like terms so cannot be collected

Factorising Quadratics

When a quadratic expression is in the form $x^2 + bx + c$ find the two numbers that add to give b and multiply to give c

$$x^2 + 7x + 10 = (x + 5)(x + 2)$$

(because 5 and 2 add to give 7 and multiply to give 10)

Algebra tiles

x^2 x 1

Positive values

Expand single brackets

$3(2x + 4)$

Different representations of $3(2x + 4) = 6x + 12$

$6x + 12$

$6x + 12$

$6x + 12$

Factorise into a single bracket

$8x + 4$

$2x + 1$

Try and make this the highest common factor

The two values multiply together (also the area) of the rectangle

$$8x + 4 \equiv 4(2x + 1)$$

Note:

$$8x + 4 \equiv 2(4x + 2)$$

This is factorised but the HCF has not been used

Directed numbers

$++ \rightarrow +$ eg $a = -5$ and $b = 2$

$-- \rightarrow +$ $a^2 = a \times a = -5 \times -5 = 25$

$+- \rightarrow -$ $b + a = 2 + -5 = -3$

$-+ \rightarrow -$

Brackets around negative substitutions helps remove calculation errors

$$2a - b = 2 \times 5 - (-4) = 10 + 4 = 14$$